



Roberto Tricarico

Tutor: Prof. Carlo Forestiere

XXXII Cycle - III year presentation

Light-Matter Interaction in Open  
Systems: from Nanoparticles to  
Atoms



UNIVERSITÀ DEGLI STUDI DI NAPOLI

FEDERICO II

# General Information

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- Bachelor's degree in electronic engineering, Università Federico II (2015)
- Master's degree in electronic engineering, Università Federico II (2016)
- ITEE: athenaeum fellowship, Prof. Carlo Forestiere

Year	Courses	Seminars	Research
1°	30	9.8	21
2°	16	9.6	34.4
3°	6	0	53.2

- **7** courses, **1** language course, **6** PhD school, **12** seminars
- **6** journal papers (+1 submitted), **2** conference papers, **2** book chapters
- **Period abroad** Third year of the PhD at the Institute of Photonic Sciences in Castelldefels (Barcelona) **ICFO**, supervised by Prof. Dr. **Darrick Chang**.
- Thesis co-supervisor : Prof. Dr. Darrick Chang.



# Course list (8)

- Ottica Quantistica (1<sup>st</sup> year)
- Meccanica Quantistica dei Molti Corpi (1<sup>st</sup> year)
- Teoria dei Gruppi e Applicazioni (1<sup>st</sup> year)
- Introduction to Quantum Electrodynamics (1<sup>st</sup> year)
- Fisica dello Stato Solido 2 (2nd year)
- Plasmonics and Metamaterials (2nd year)
- Elettromagnetismo e Relatività (2nd year)
- Spanish course (A1) (3rd year)

• Estimated • Achieved

	Credits year 1						Credits year 2						Credits year 3						TOTAL							
	1	2	3	4	5	6	1	2	3	4	5	6	1	2	3	4	5	6								
Modules	30	8	3	11	0	0	8	30	20	0	8	4	0	0	4	16	0	3	0	3	0	0	0	6	30-70	52
Seminars	10	0.4	0	0.4	6	3	0	9.8	10	0	2.3	3.5	0	3.8	0	9.6	0	0	0	0	0	0	0	0	10-30	19.4
Research	20	3	5	3	3	6	1	21	30	8	3	3	8	7.4	5	34.4	60	7	10	6.2	10	10	10	53.2	80-140	108.6
	60	11	8	14	9	9	9	60.8	60	8	13.3	10.5	8	11.2	9	60	60	10	10	9.2	10	10	10	59.2	180	180



# PhD school list (6)

- Antenna Synthesis, Napoli, (1<sup>st</sup> year)
- Ferdinando Gasparini XXI edizione, Napoli, (1<sup>st</sup> year)
- XLII Scuola estiva di Fisica Matematica, Ravello, (1<sup>st</sup> year)
- International School of Plasmonics and Nano-Optics, Cetraro, (2nd year)
- Ferdinando Gasparini XXII edizione, Napoli, (2nd year)
- Light Matter interaction in Dilute Media and Individual Quantum Systems, Les Houches, (3rd year)

• Estimated • Achieved

	Credits year 1						Credits year 2						Credits year 3						TOTAL							
	1	2	3	4	5	6	1	2	3	4	5	6	1	2	3	4	5	6								
Modules	30	8	3	11	0	0	8	30	20	0	8	4	0	0	4	16	0	3	0	3	0	0	0	6	30-70	52
Seminars	10	0.4	0	0.4	6	3	0	9.8	10	0	2.3	3.5	0	3.8	0	9.6	0	0	0	0	0	0	0	0	10-30	19.4
Research	20	3	5	3	3	6	1	21	30	8	3	3	8	7.4	5	34.4	60	7	10	6.2	10	10	10	53.2	80-140	108.6
	60	11	8	14	9	9	9	60.8	60	8	13.3	10.5	8	11.2	9	60	60	10	10	9.2	10	10	10	59.2	180	180



# Seminar list (12)

- Electromechanical Consequences of Violent Instabilities in Tokamaks, Vladimir D. Pustovitov
- Smart Nanodevices for Theranostics, Ilaria Rea
- Magnetic Refrigeration: Thermodynamics of novel magnetic materials for an efficient cooling technique, Vittorio Basso
- Thermodynamics in spintronics: the spin Seebeck and spin Peltier effects, Vittorio Basso
- Approssimazioni di problemi alle derivate parziali e applicazioni, Alfio Quarteroni
- Tailoring Waves at the extreme with metamaterials, Nader Engheta
- Near-zero-index photonics, Nader Engheta
- IBM Q: building the first universal quantum computers for business and science, Federico Mattei and Najla Said
- How to Produce a scientific paper, Aliaksandr Birokou and Elisa Magistrelli
- Tomografia e Imaging: Principi, Algoritmi e Metodi Numerici, Pasquale Memmolo
- The power of Trefftz Approximations: Applications in Electromagnetics, Igor Tsukerman
- Non-Asymptotic and Nonlocal Homogenization of Periodic Electromagnetic Structures , Igor Tsukerman

• Estimated • Achieved

	Credits year 1						Credits year 2						Credits year 3						TOTAL							
	1	2	3	4	5	6	1	2	3	4	5	6	1	2	3	4	5	6								
Modules	30	8	3	11	0	0	8	30	20	0	8	4	0	0	4	16	0	3	0	3	0	0	0	6	30-70	52
Seminars	10	0.4	0	0.4	6	3	0	9.8	10	0	2.3	3.5	0	3.8	0	9.6	0	0	0	0	0	0	0	0	10-30	19.4
Research	20	3	5	3	3	6	1	21	30	8	3	3	8	7.4	5	34.4	60	7	10	6.2	10	10	10	53.2	80-140	108.6
	60	11	8	14	9	9	9	60.8	60	8	13.3	10.5	8	11.2	9	60	60	10	10	9.2	10	10	10	59.2	180	180



# Publication list

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## Journal papers (6)

- C. Forestiere, G. Miano, G. Rubinacci, A. Tamburrino, R. Tricarico, S. Ventre, “Material-Independent Modes of Arbitrarily Shaped Homogeneous Scatterers”, **IEEE Transactions on Antennas and Propagation**, Mar. 2018
- C. Forestiere, G. Miano, M. Pascale, R. Tricarico, “Directional scattering cancellation for an electrically large dielectric sphere”, **Optics Letters**, Apr. 2019
- C. Forestiere, G. Miano, M. Pascale, R. Tricarico, “Electromagnetic modes and resonances of two-dimensional bodies”, **Phys. Rev. B**, Apr. 2019
- C. Forestiere, G. Miano, M. Pascale and R. Tricarico, “Electromagnetic Scattering Resonances of Quasi-1-D Nanoribbons”, **IEEE Transactions on Antennas and Propagation**, Aug. 2019
- M. Pascale, G. Miano, R. Tricarico, and C. Forestiere, “Full-wave electromagnetic modes and hybridization in nanoparticle dimers”, **Scientific Reports**, Oct. 2019
- C. Forestiere, G. Miano, M. Pascale, G. Rubinacci, A. Tamburrino, R. Tricarico, and S. Ventre, "Magnetoquasistatic Resonances of Small Dielectric Objects." Accepted by **Physical Review Research**

# Publication list

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## Conference papers (2)

- M. Pascale, R. Tricarico, G. Miano and C. Forestiere, Full-wave mode hybridization in nanoparticle dimers, 2019 International Conference on Electromagnetics in Advanced Applications (**ICEAA 19**), Granada, Spain, 2019.
- R. Tricarico, C. Forestiere, G. Miano and M. Pascale, Field Quantization in Arbitrarily-Shaped Metal Nanoparticles, International Conference on Electromagnetics in Advanced Applications (**ICEAA 19**), Granada, Spain, 2019.

## Book Chapters (2)

- C. Forestiere, G. Miano, M. Pascale, R. Tricarico, chapter title: “A full-retarded spectral technique for the Fano-resonance analysis in a dielectric nanosphere”, **Springer** book: “Fano Resonances in Optics and Microwaves”, pp. 185-218, Nov. 2018.
- C. Forestiere, G. Miano, M. Pascale, R. Tricarico, chapter title: “Material Independent Modes for the design of electromagnetic scattering”, **World Scientific Publishing** book: “Compendium on Electromagnetic Analysis – from electrostatics to photonics: fundamentals and applications for physicists and engineers”, out in Apr. 2020.

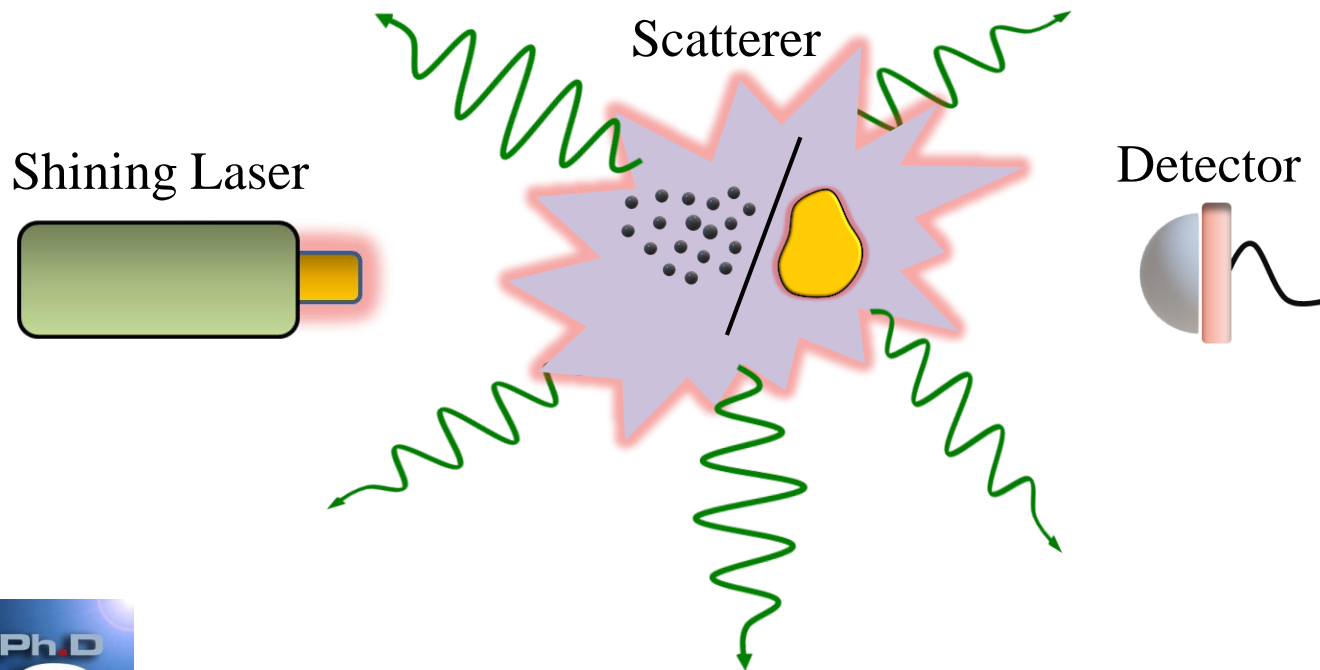
## Submitted paper (1)

- C. Forestiere, G. Miano, M. Pascale and R. Tricarico, “Quantum theory of Radiative Decay Rate and Frequency Shift of Surface Plasmon Modes in Arbitrarily Shaped Nanoparticles”, **arXiv**, Jan. 2020.



# Light-Matter in Open Systems

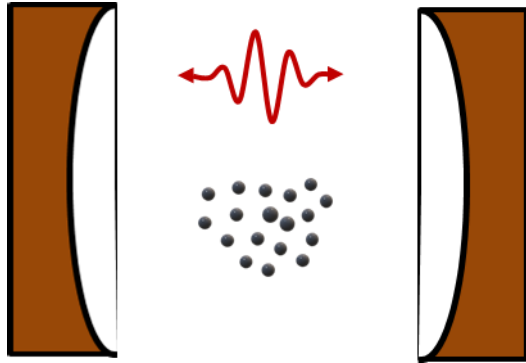
The study of the interaction between light and matter at the nano/atomic scale presents interesting challenges and new perspective in the case of **open systems**, i.e. systems which **lose energy** (radiation to infinity).





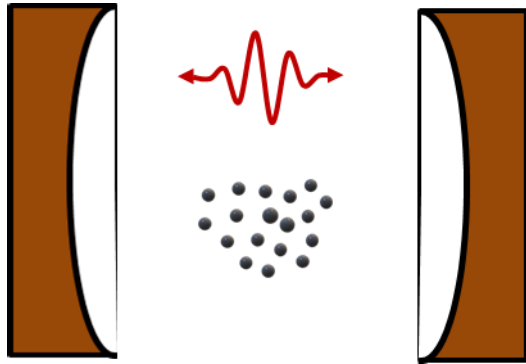
# Open Systems: Atoms

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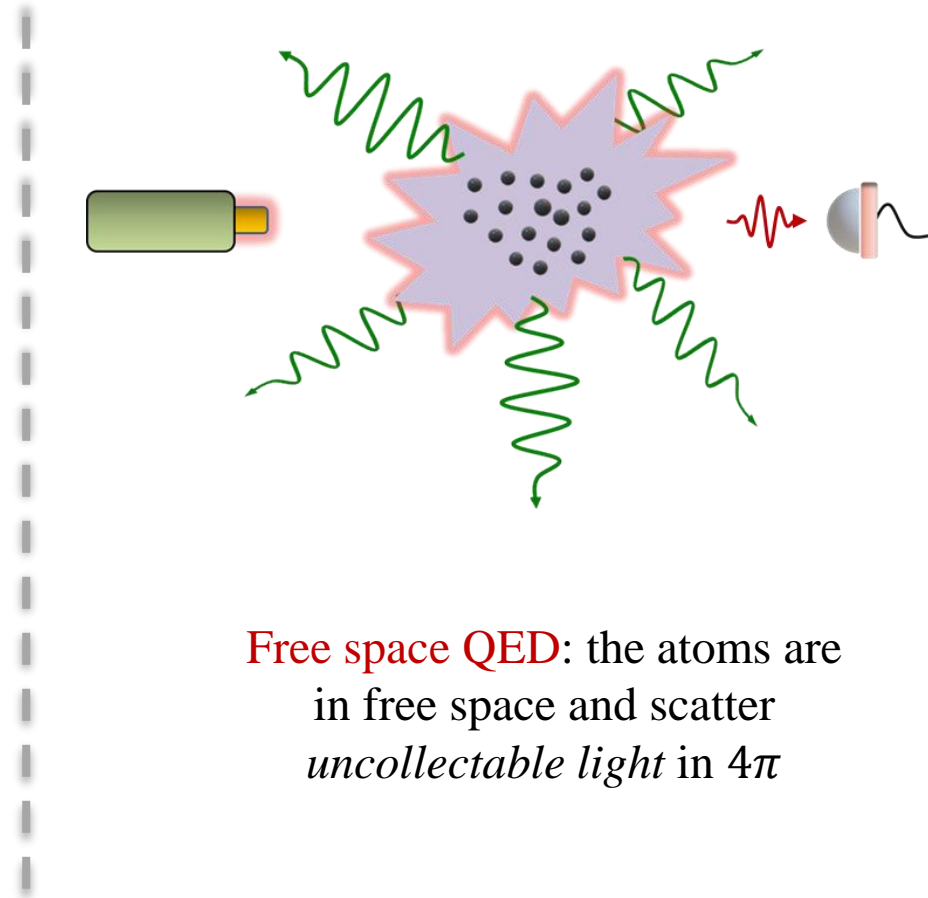


Cavity-QED: the atoms are enclosed in an optical cavity (*closed system*)

# Open Systems: Atoms



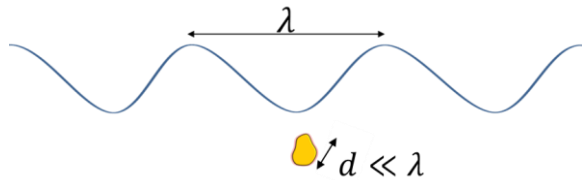
**Cavity-QED:** the atoms are enclosed in an optical cavity (*closed system*)



**Free space QED:** the atoms are in free space and scatter *uncollectable light* in  $4\pi$

# Open Systems: Nanoparticles

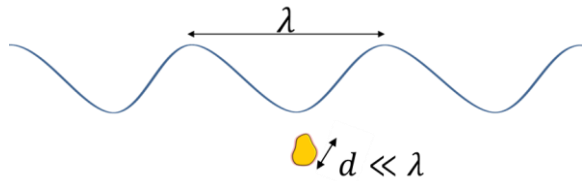
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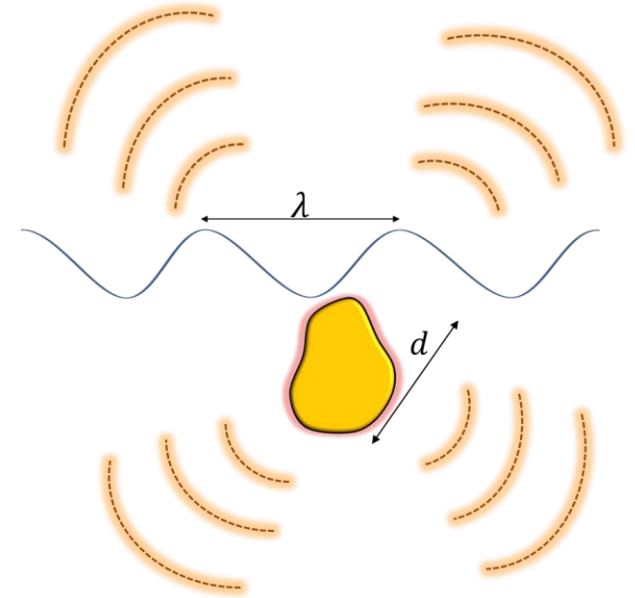
Quasistatic limit:  $d \ll \lambda$  retarded  
NO RADIATION OF ENERGY TO  
INFINITY (*closed system*)



# Open Systems: Nanoparticles



Increasing  $d$   
➔



**Quasistatic** limit:  $d \ll \lambda$  retarded  
NO RADIATION OF ENERGY TO  
INFINITY (*closed system*)

**Full-retarded** limit:  $d \sim \lambda$   
RADIATION OF ENERGY TO  
AT INFINITY (*Open System*)

# Light-Matter in Open Systems

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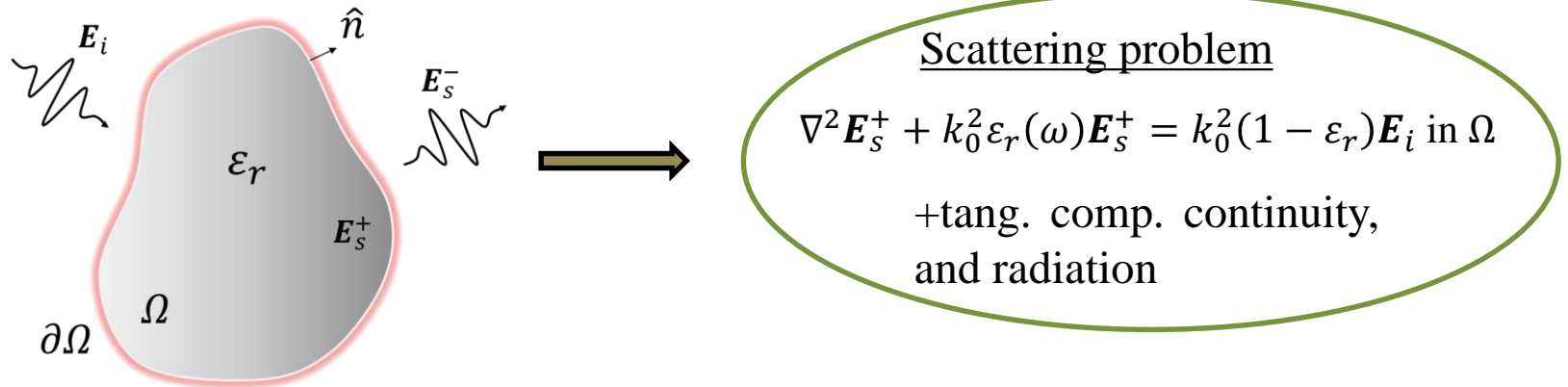
*Three* selected topics in Light-Matter Interaction in Open Systems

**I** Material Independent Modes for  
the Electromagnetic Scattering  
*NANOPARTICLES, Classical  
Electrodynamics*

**II** Quantum theory of frequency shift  
and radiative decay rate in arbitrarily  
shaped metal nanoparticles and dimers  
*NANOPARTICLES, Quantum  
Electrodynamics*

**III** Nonlinearities in Rydberg-EIT,  
*ATOMS*

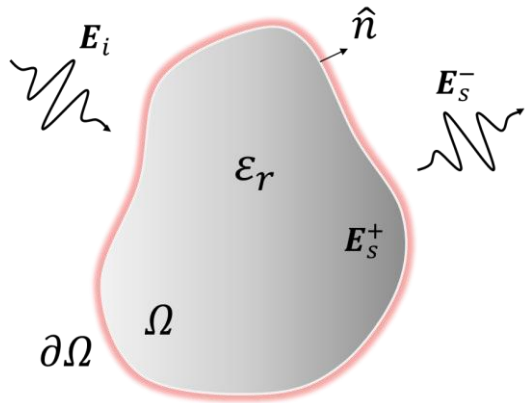
# I Material Independent Modes



We *don't want* to solve the problem **directly**, but we *want* to provide a **modal theory** for the scattering in open systems:

- to have more insight on the **physics**
- for a rigorous understanding of the **interference** patterns (*analysis*)
- to simplify the material **design** of the scattered in to maximize assigned scattering features (*synthesis*)

# I Material Independent Modes



## Scattering problem

$$\nabla^2 \mathbf{E}_s^+ + k_0^2 \epsilon_r(\omega) \mathbf{E}_s^+ = k_0^2 (1 - \epsilon_r) \mathbf{E}_i \text{ in } \Omega$$

+tang. comp. continuity,  
and radiation

## Linear algebra analogy

$$Ax = b,$$
$$A = A^+$$

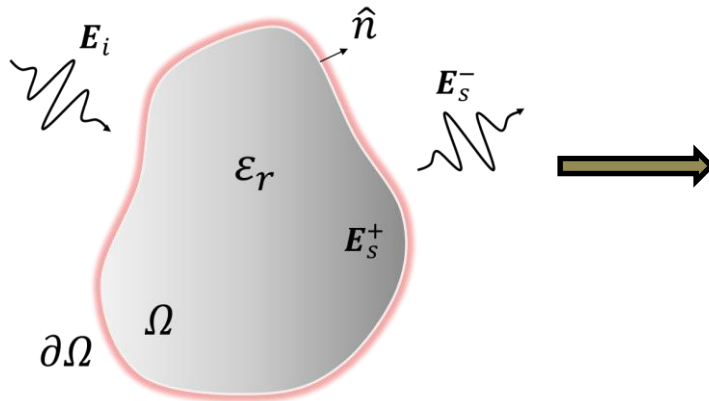
## Direct solution

$$x = A^{-1}b$$

## Modal solution

$$Ac_i = \lambda_i c_i \quad x = \sum_i \frac{1}{\lambda_i} \frac{\langle c_i, b \rangle}{\langle c_i, c_i \rangle} c_i$$

# I Material Independent Modes



## Scattering problem

$$\nabla^2 \mathbf{E}_s^+ + k_0^2 \epsilon_r(\omega) \mathbf{E}_s^+ = k_0^2 (1 - \epsilon_r) \mathbf{E}_i \text{ in } \Omega$$

+tang. comp. continuity,  
and radiation

## Auxiliary eigenvalue problem

$$-\frac{1}{k_0^2} \nabla^2 \mathbf{C}_r = -\gamma_r \mathbf{C}_r \text{ in } \Omega$$

+tang. comp. continuity,  
and radiation

It is **MATERIAL INDEPENDENT**

## Modal solution

$$\mathbf{E}_s^+ = (1 - \epsilon_r) \sum_r \frac{1}{\epsilon_r - \gamma_r} \frac{\langle \mathbf{C}_r^*, \mathbf{E}_i \rangle}{\langle \mathbf{C}_r^*, \mathbf{C}_r \rangle} \mathbf{C}_r$$

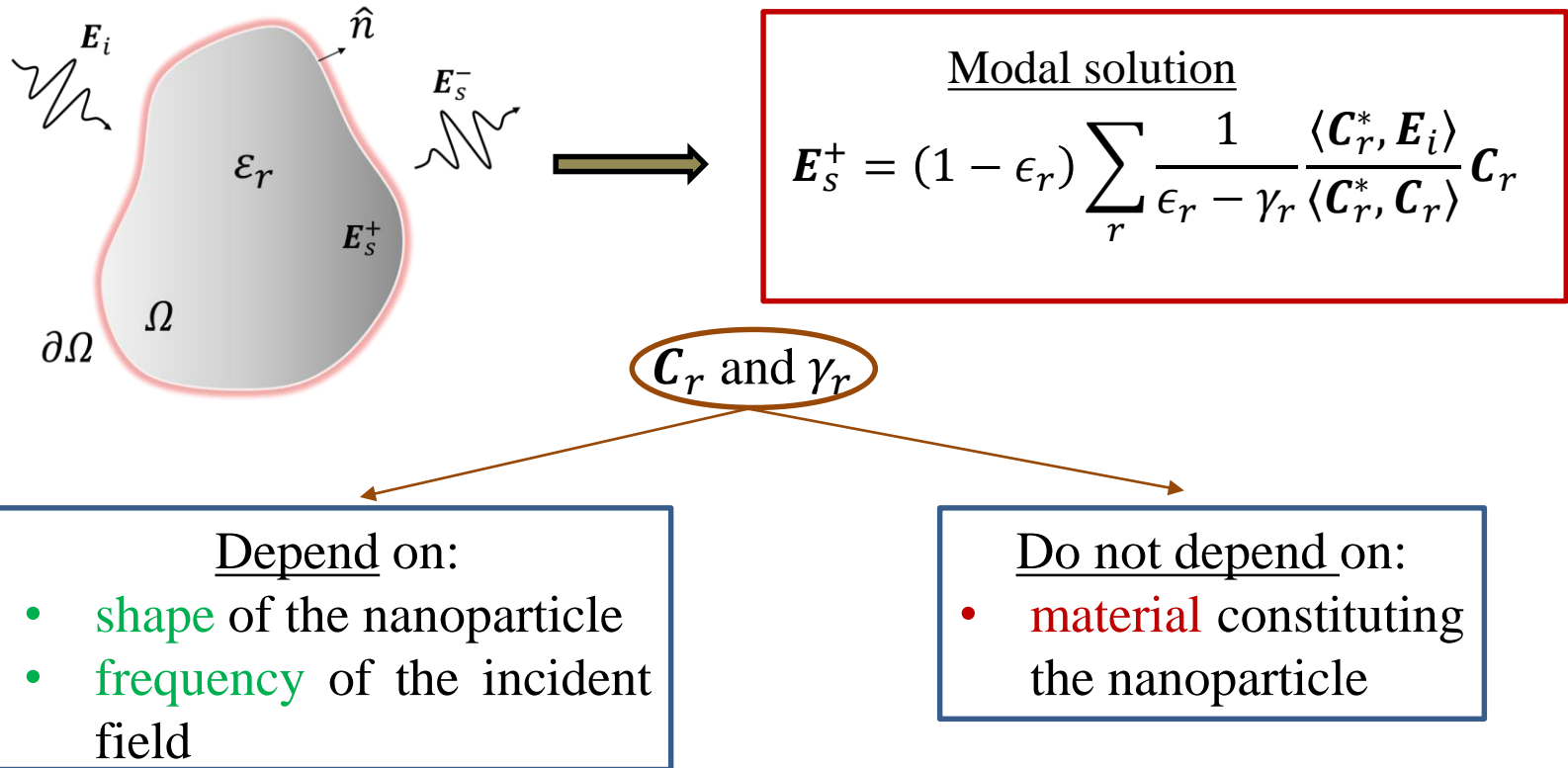
where  $\langle \mathbf{A}, \mathbf{B} \rangle = \int_{\Omega} \mathbf{A}^* \cdot \mathbf{B} d\Omega$

Material

Geometry



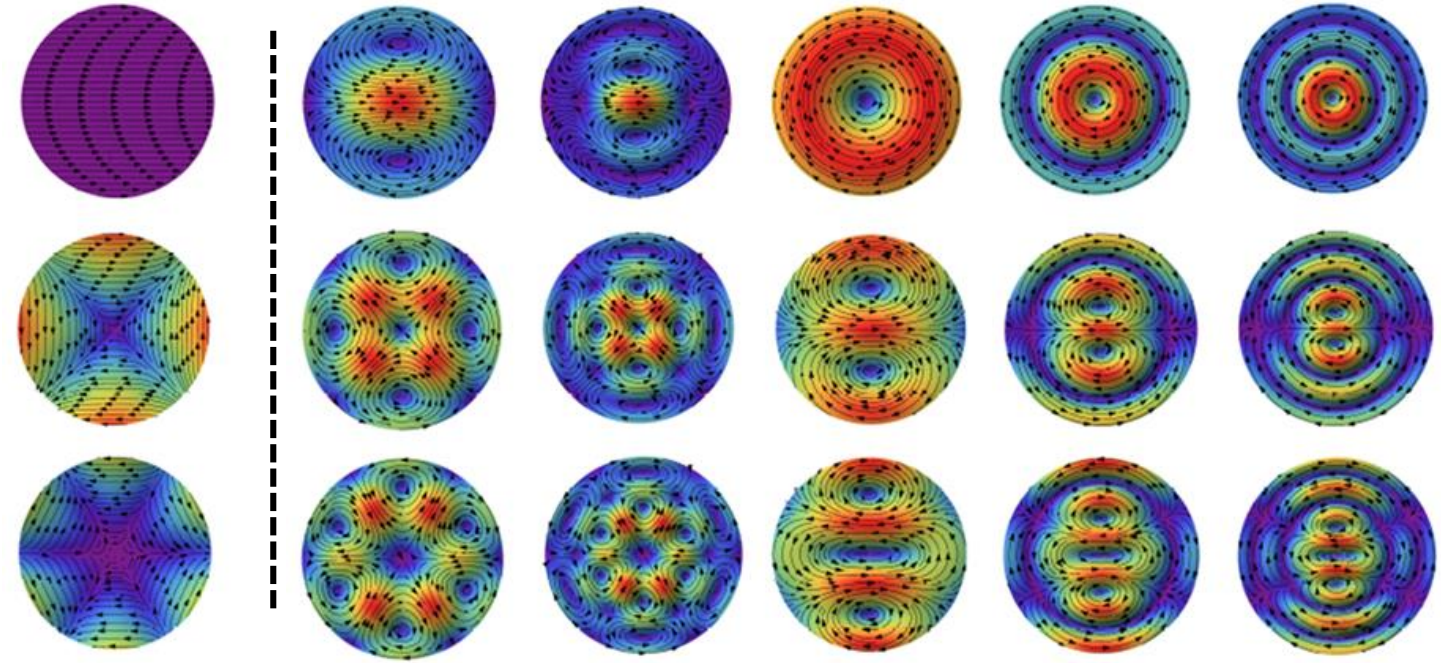
# I Material Independent Modes



Material Resonance  $\longrightarrow$   $\min|\epsilon_r - \gamma_r|$

# I MIM: isolated sphere

Material  
Independent  
Modes  $C_r$



Plasmonic Modes

- Sources and sinks

Photonic Modes

- Vortices

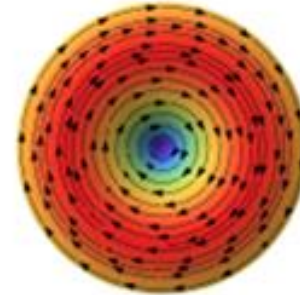
# I MIM: isolated sphere

## Plasmonic Mode

## Photonic Mode

Eigen-permittivities

$\gamma_r$

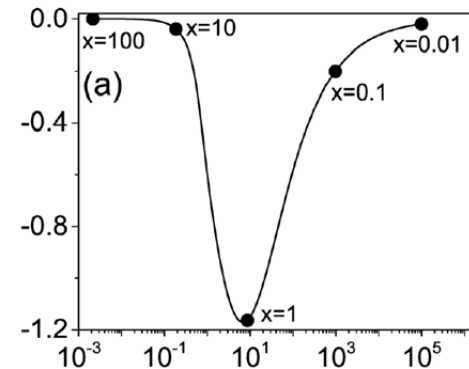
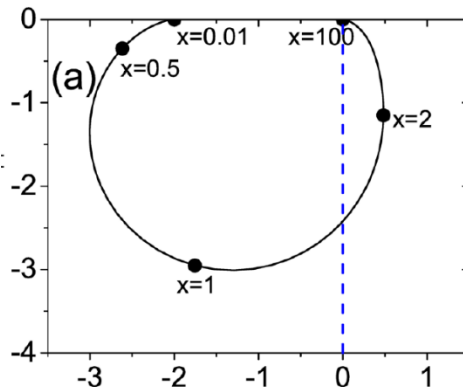


- $\gamma$  in the III quadrant
- Can resonate in *plasmons* ( $\text{Re}[\epsilon_r] < 0$ )

- $\gamma$  in the IV quadrant
- Can resonate in *dielectrics* ( $\text{Re}[\epsilon_r] > 0$ )

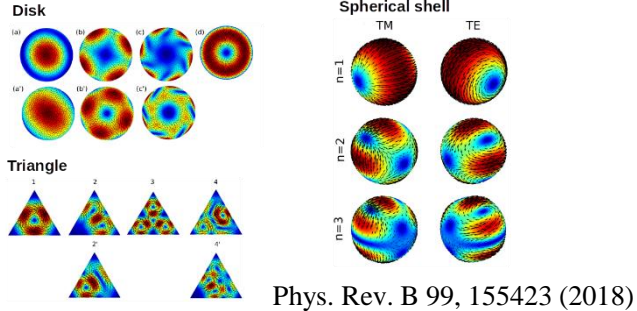
Size parameter

$$x = \frac{2\pi R}{\lambda}$$

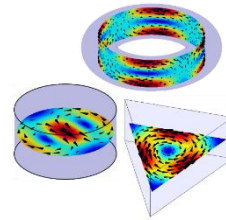


# I MIM: what done so far

## 2D-structures

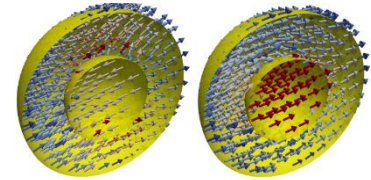


## High-index dielectrics



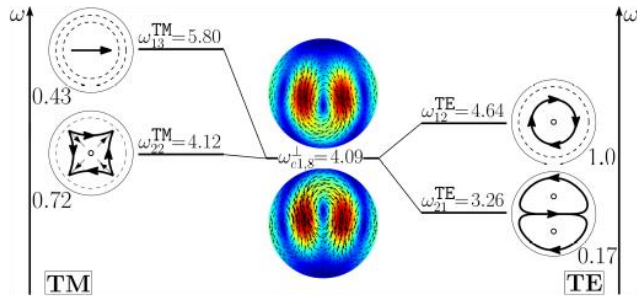
Physical Review Research (2020)

## Electromagnetic coating



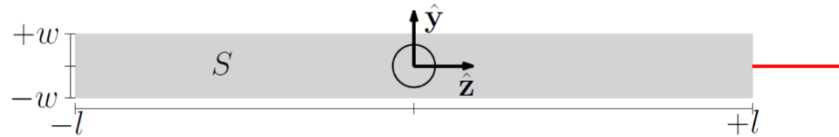
J. Opt. Soc. Am. B 34, 1524-1535 (2017)  
Opt. Lett. 44, 1972-1975 (2019)

## Hybridization theory



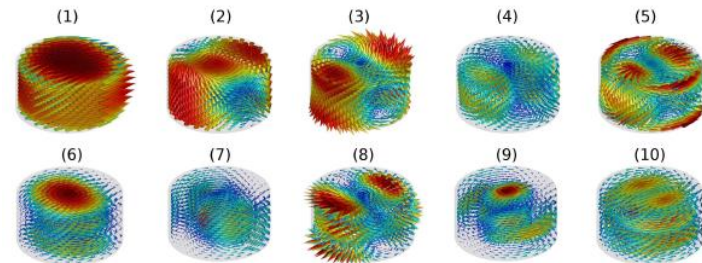
Sci Rep 9, 14524 (2019)

## Quasi-1D nanoribbon



IEEE Transactions on Antennas and Propagation, vol. 67, no. 8, pp. 5497-5506 (2018)

## Arbitrary shaped nanoparticle



IEEE Transactions on Antennas and Propagation, vol. 66, pp. 2505-2514 (2018)

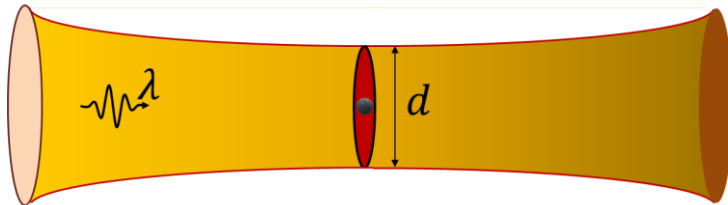
# II Plamon quantization: why?

## Statement

At the basis of many new applications in quantum technology, such as single-photon nonlinear optics, nonclassical states of light, photonic gates and others, there is the need of reaching an efficient atom-photon interaction.

## Issue

The atoms, due to the low scattering cross section, don't like to interact with light.



$$p \approx \frac{\sigma}{d^2} \approx \frac{\lambda^2}{d^2} \ll 1$$

Plasmonic structure can localize light beyond the diffraction limit

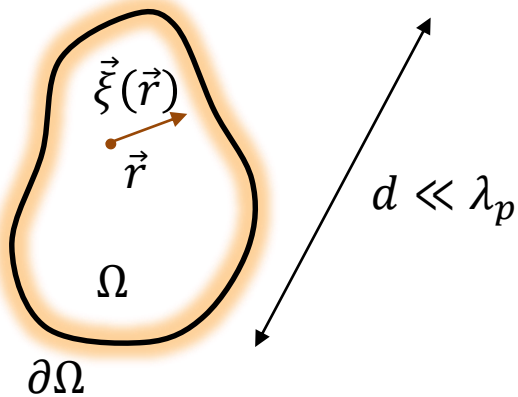
$d \downarrow$

A proper quantum description of the localized plasmon NPs

- is needed in some conditions (e.g. strong coupling regime in the analysis of quantum emitters)
- can give a real insight in the physics of the phenomenon



# II Plamon quantization (closed/quasistatic)



$\xi(\mathbf{r})$  Electron displacement field

$n_0$  electron density at rest,  
 $m_e$  electron effective mass,  
 $\lambda_p$  plasmon wavelength

$$E = \underbrace{\int_B \frac{1}{2} m_e n_0 |\partial_t \vec{\xi}|^2}_{\text{Kinetic energy}} + \underbrace{\frac{(en_0)^2}{8\pi\epsilon_0} \int_S \int_S \frac{\xi_n(\vec{r}) \xi_n(\vec{r}')}{|\vec{r} - \vec{r}'|}}_{\text{Coulomb energy}}$$

$$\vec{\xi}(\vec{r}, t) = \sum_m q_m(t) \vec{U}_m(\vec{r})$$

$$(p_m = m_e \dot{q}_m)$$

$$H(q_m, p_m) = \sum_n \left( \frac{p_m^2}{2M_m} + \frac{1}{2} M_m \Omega_m^2 q_m^2 \right)$$

Plasmon modes

$$\begin{aligned} \nabla \times \vec{U}_m &= 0 \\ \nabla \cdot \vec{U}_m &= 0 \\ \vec{U}_m \cdot \hat{n} \Big|_S &\neq 0 \end{aligned}$$

Plasmon frequency

$$\Omega_m$$

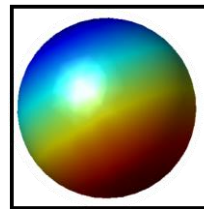
Plasmon mass

$$M_m = m_e n_0 V_m$$

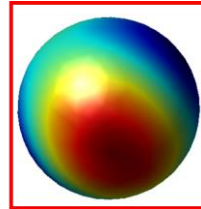
Plasmon volume

$$V_m = \langle \vec{U}_m, \vec{U}_m \rangle$$

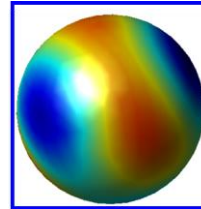
$m = 1$



$m = 2$



$m = 3$

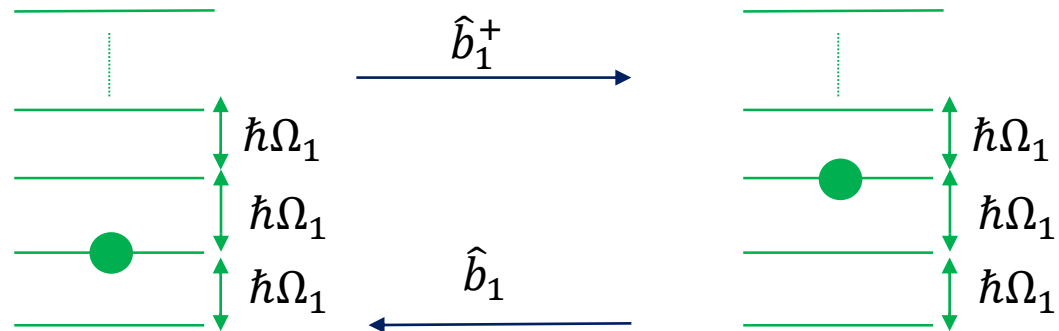
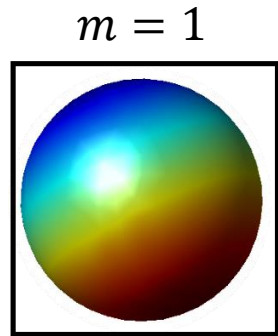


Surface charges

# II Plamon quantization (closed/quasistatic)

$$H = \sum_n \left( \frac{p_m^2}{2M_m} + \frac{1}{2} M_m \Omega_m^2 q_m^2 \right) \longrightarrow \hat{H}_M = \sum_m \hbar \Omega_m \left( \hat{b}_m^+ \hat{b}_m + \frac{1}{2} \right)$$

Canonical Quantization

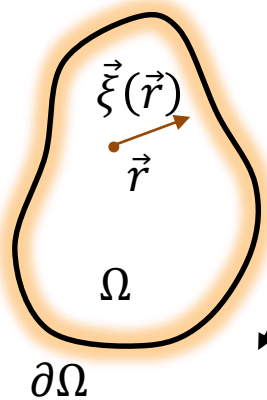


## Definition of plasmon

A quantum of energy in the collective motion of electron.

- Infinite lifetime
- Energy  $\hbar \Omega_m$

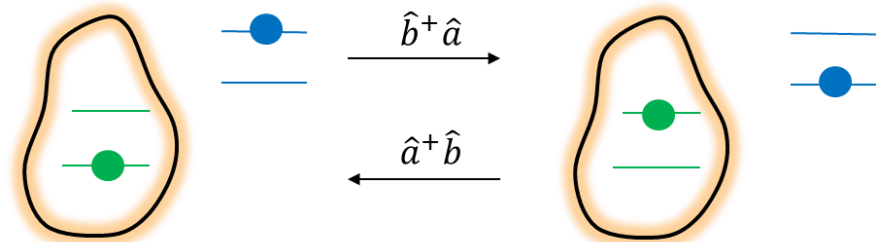
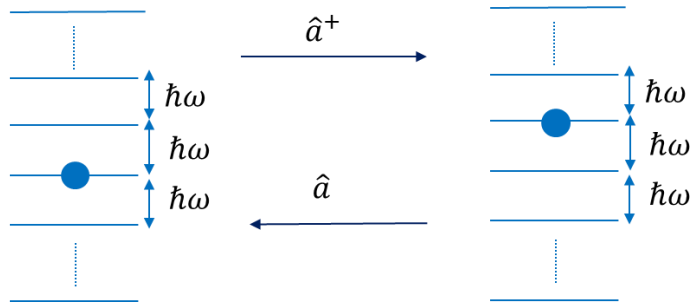
# II Plamon quantization (open/retarded)



$$\hat{H} = \hat{H}_M + \hat{H}_{EM} + \hat{H}_I + \hat{H}_{II}$$

$$\int_{R_3} \frac{d^3 \vec{q}}{(2\pi)^3} \sum_{s=1,2} \hbar \omega_{\vec{q},s} \left( \hat{a}_{\vec{q},s}^+ \hat{a}_{\vec{q},s} + \frac{1}{2} \right)$$

$$\sum_m \int_{R_3} \frac{d^3 \vec{q}}{(2\pi)^3} \sum_{s=1,2} [V_{\vec{q},s}^m (\hat{b}_m^+ - \hat{b}_m) \hat{a}_{\vec{q},s} + h.c.]$$





# II Plamon quantization (open/retarded)

Approximate plasmon-photon interaction (independent modes)

$$\hat{H} = \hat{H}_M + \hat{H}_{EM} + \hat{H}_I$$

- The plasmon excitations decay in time  $\tau_m = 1/\Gamma_m$
- The plasmon energies shift  $\hbar\Omega_m \rightarrow \hbar\Omega_m + \hbar\Delta\Omega_m$

$$\Gamma_m = -Im \left[ \Omega_m \sqrt{1 + \frac{2\Psi(\Omega_m)}{\hbar\Omega_m}} \right] \quad \Delta\Omega_m = -Im \left[ \Omega_m \sqrt{1 + \frac{2\Psi(\Omega_m)}{\hbar\Omega_m}} \right]$$

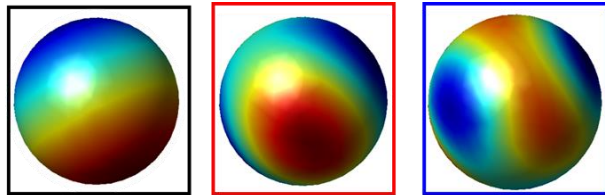
Full-retarded quantities

$$\Psi(\Omega_m) = \frac{1}{\hbar} \int \frac{d^3\vec{q}}{(2\pi)^3} \sum_{s=1,2} |V_{\vec{q},s}|^2 \left[ p.v. \frac{1}{\Omega_m - \omega_q} - \frac{1}{\Omega_m + \omega_q} - i\pi\delta(\Omega_m - \omega_q) \right]$$

Non-perturbative

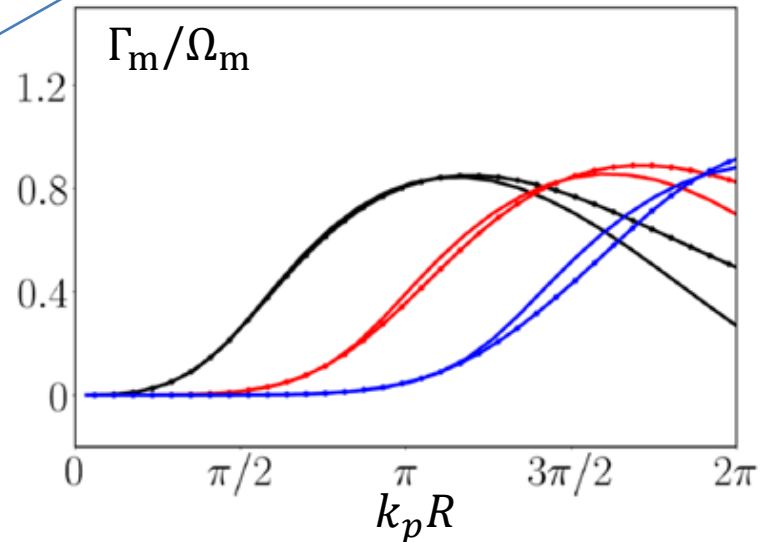
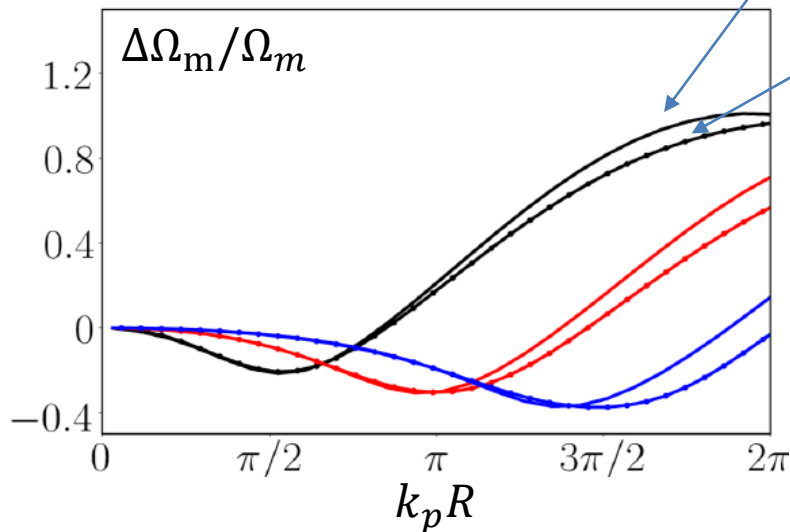
quasistatic computation

# II Plamon quantization (open/retarded)



Exact solution

Approximate solution



$$k_p = 2\pi/\lambda_p$$

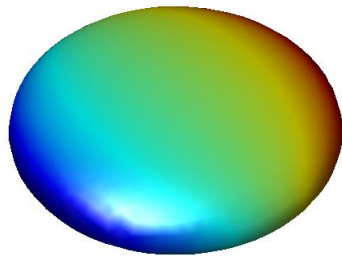
It is essentially exact for  $k_p R < \pi$

Ex. Gold  $k_p R = \pi$  means  $R = 144$  nm

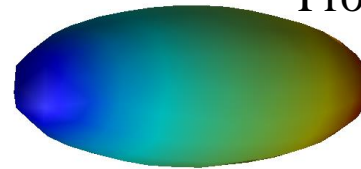
Silver  $k_p R = \pi$  means  $R = 230$  nm

# II Plasmon quantization (open/retarded)

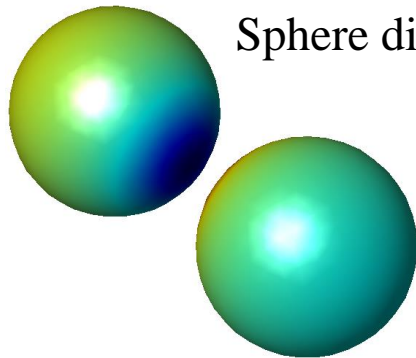
This theory has been applied to compute the *radiative decay rate* and the *frequency shift* of the plasmon oscillations in **arbitrary shaped** nanoparticles and dimers.



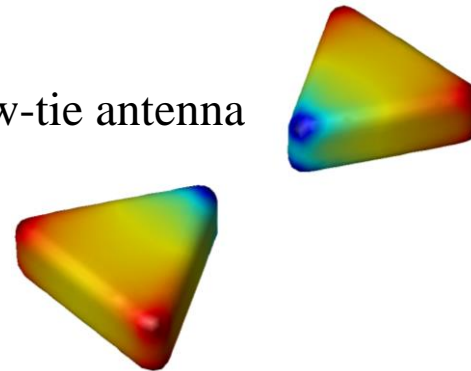
Oblate spheroid



Prolate spheroid



Sphere dimer



Bow-tie antenna

# III Photon-photon interaction

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Photons in linear media do not interact



Effective photon-photon interaction exploiting the *nonlinearity of the atoms*

$|e\rangle$  —

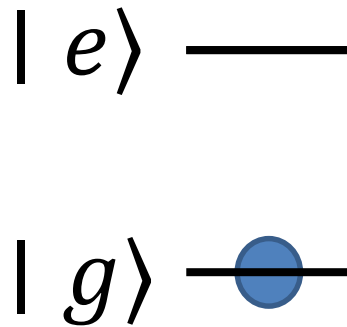
$|g\rangle$  —●

# III Photon-photon interaction

Photons in linear media do not interact



Effective photon-photon interaction exploiting the *nonlinearity of the atoms*



# III Photon-photon interaction

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Effective photon-photon interaction exploiting the *nonlinearity of the atoms*

$|e\rangle$

$|g\rangle$

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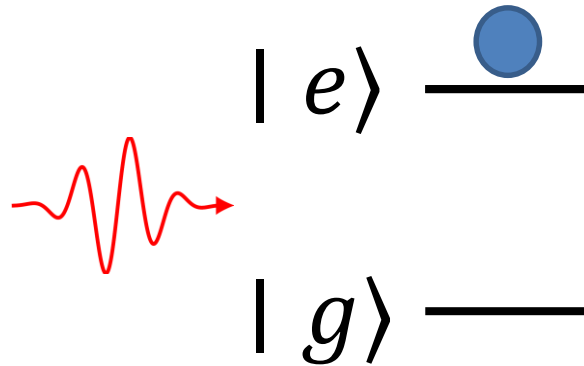
$|g\rangle$

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Photons in linear media do not interact



Effective photon-photon interaction exploiting the *nonlinearity of the atoms*



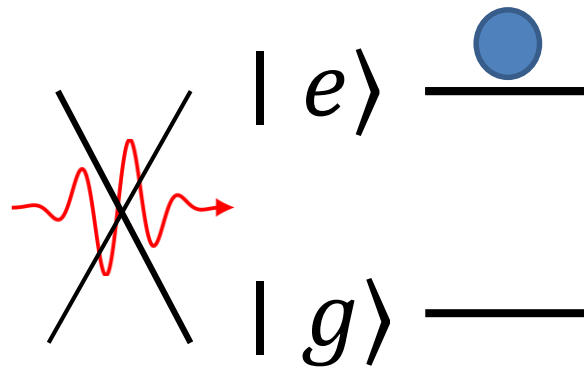


# III Photon-photon interaction

Photons in linear media do not interact



Effective photon-photon interaction exploiting the *nonlinearity of the atoms*



Blockade phenomenon

Another photon cannot be absorbed!

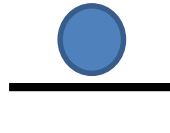
# III Photon-photon interaction

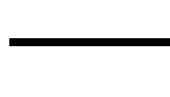
Photons in linear media do not interact



Effective photon-photon interaction exploiting the *nonlinearity of the atoms*

But in real life the probability of interaction is too small!

$|e\rangle$  

$|g\rangle$  

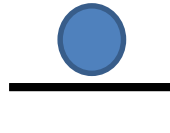
# III Photon-photon interaction

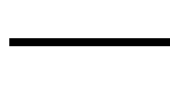
Photons in linear media do not interact



Effective photon-photon interaction exploiting the *nonlinearity of the atoms*

But in real life the probability of interaction is too small!

$|e\rangle$  

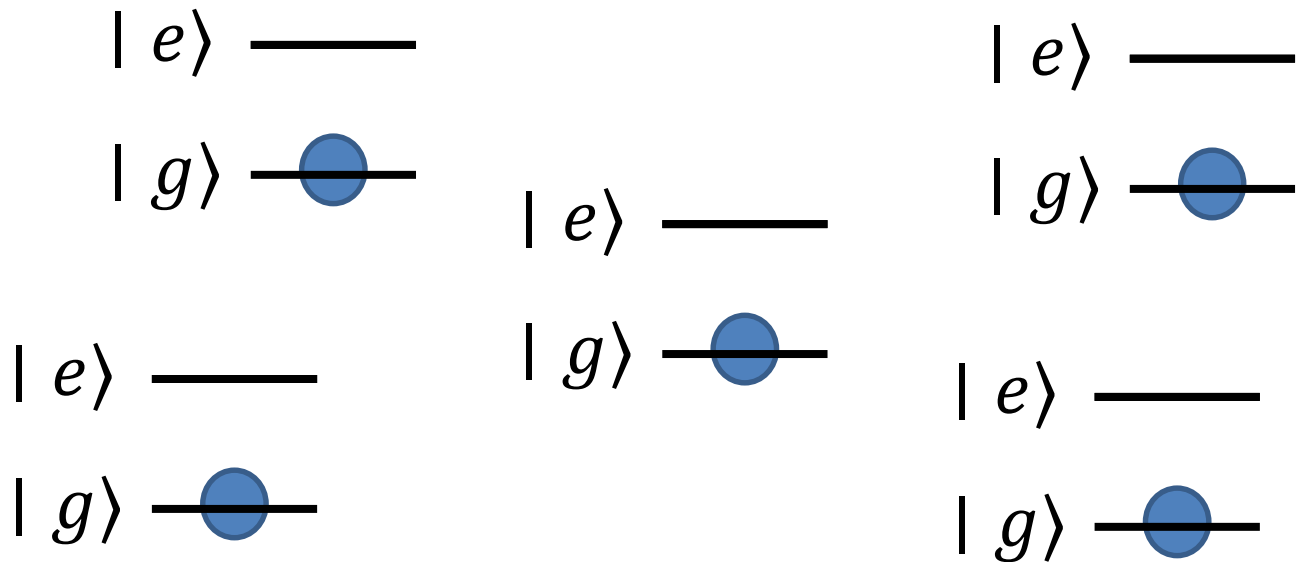
$|g\rangle$  

# III Photon-photon interaction

Photons in linear media do not interact



Effective photon-photon interaction exploiting the *nonlinearity of the atoms*

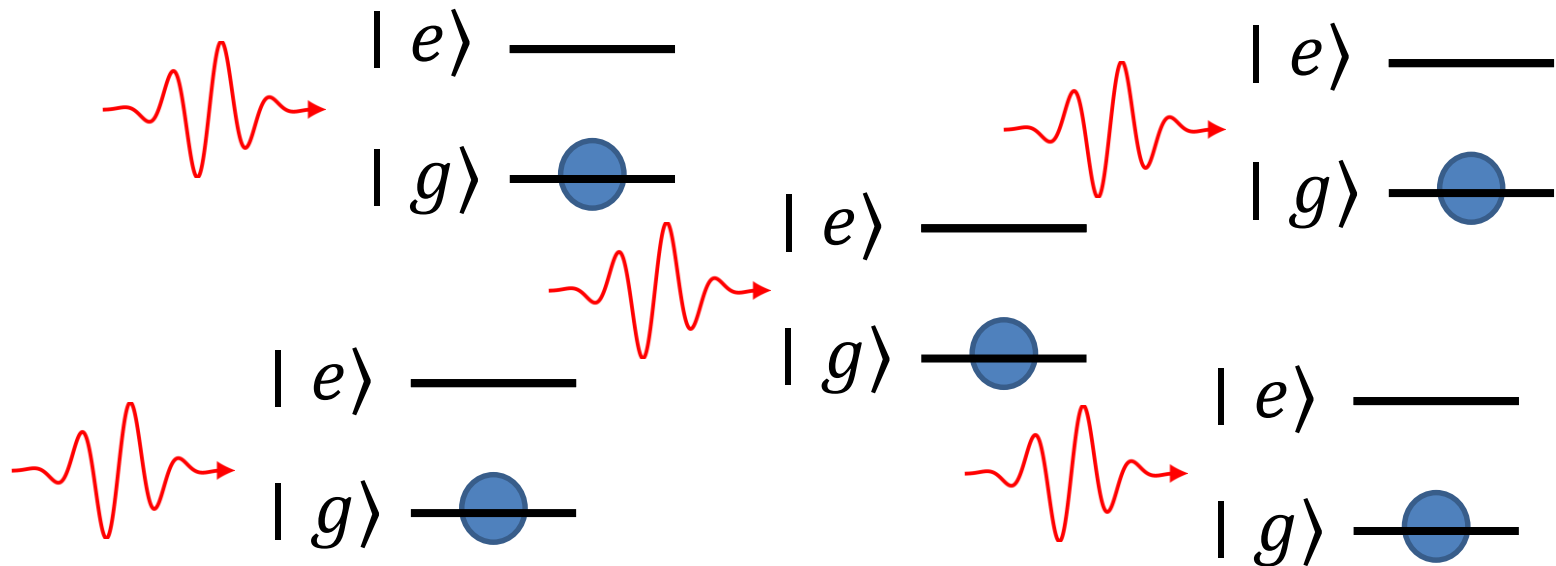


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Effective photon-photon interaction exploiting the *nonlinearity of the atoms*

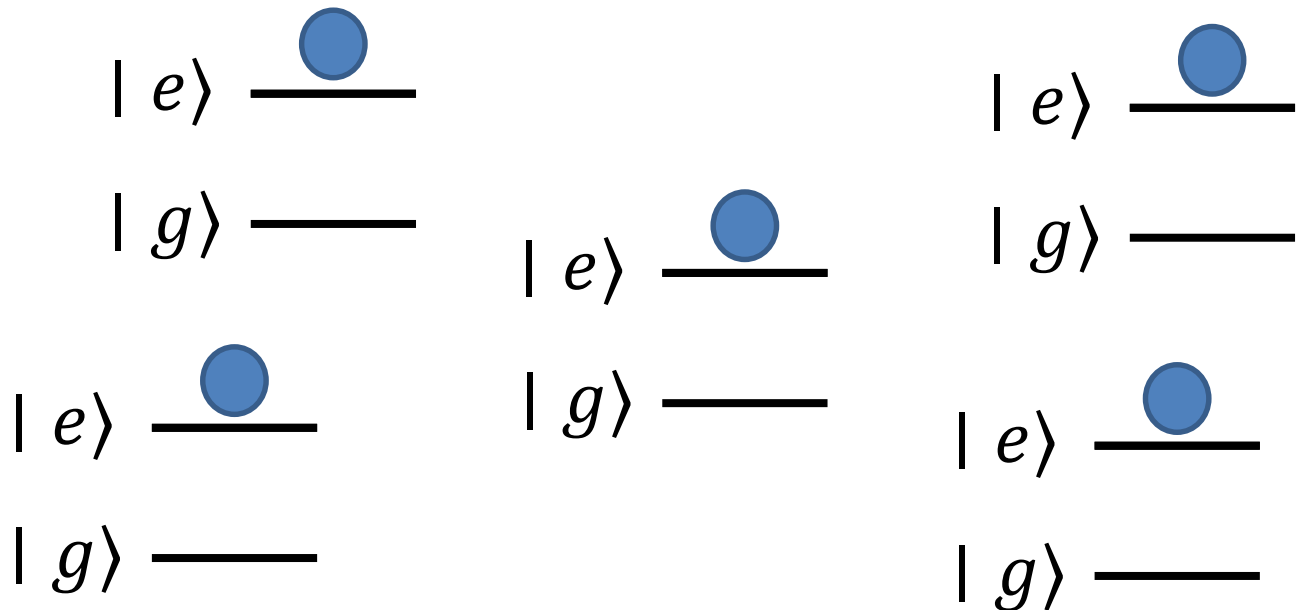


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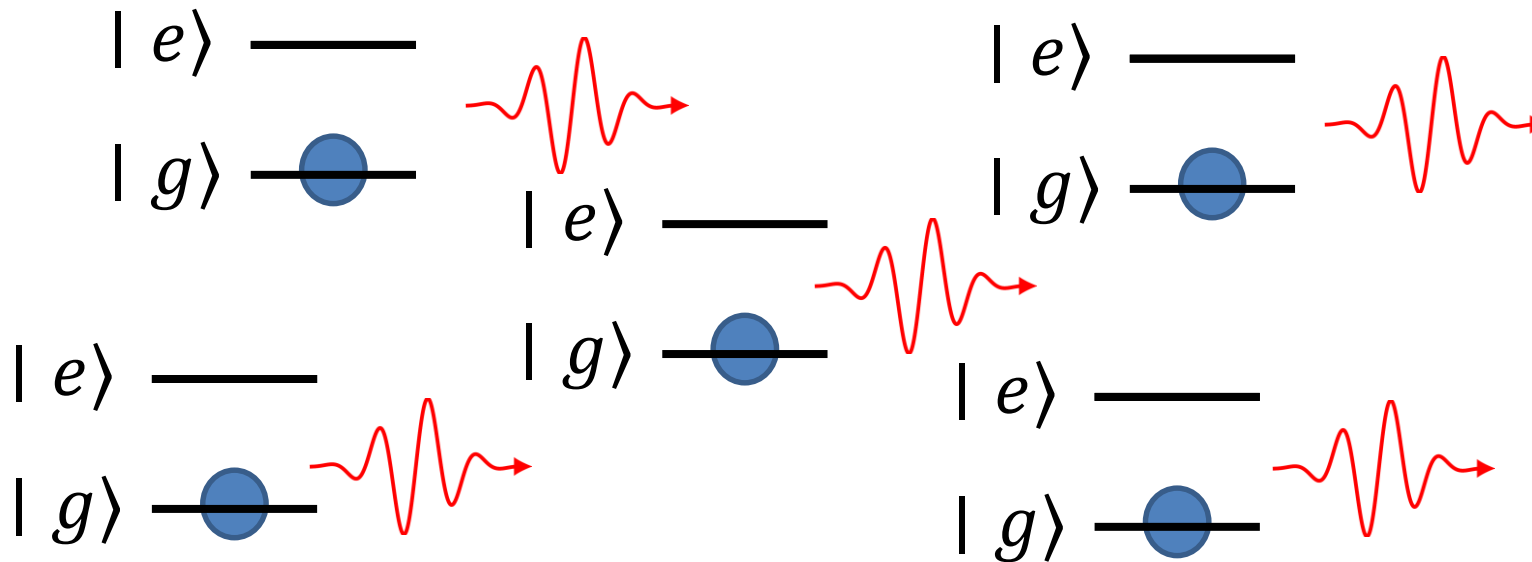


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Effective photon-photon interaction exploiting the *nonlinearity of the atoms*

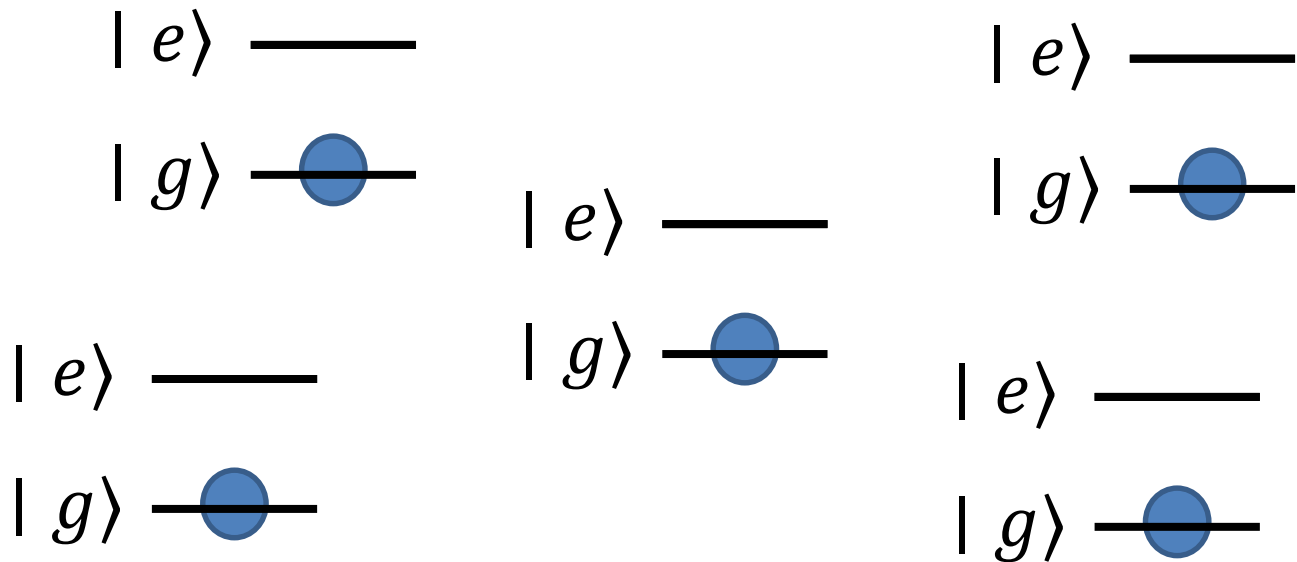


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Effective photon-photon interaction exploiting the *nonlinearity of the atoms*



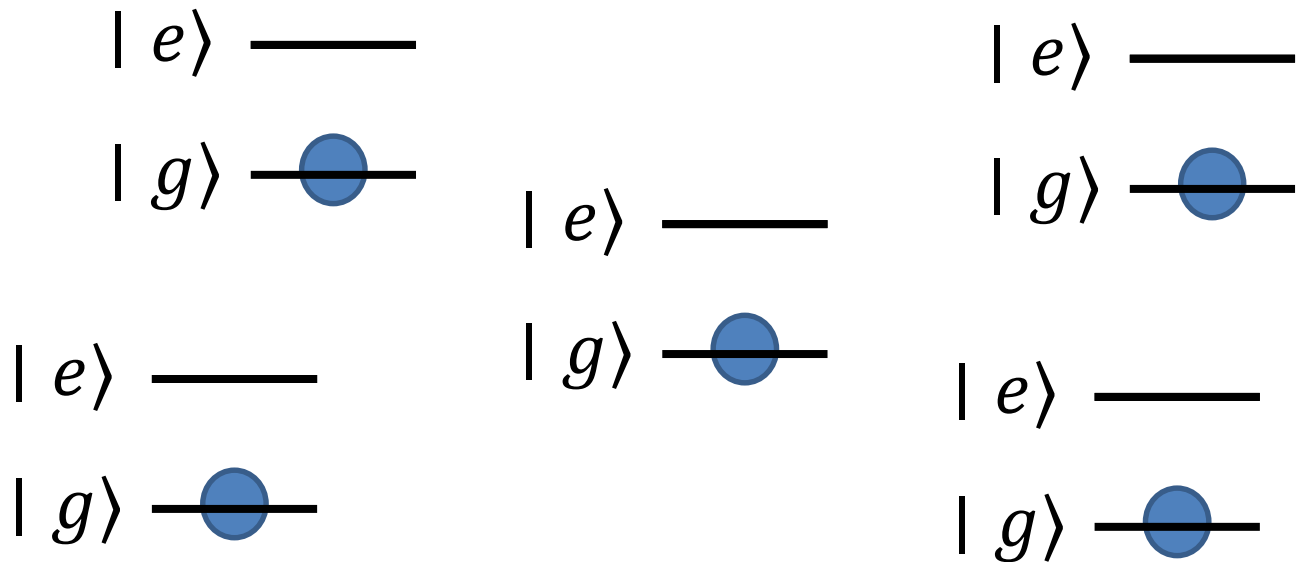


# III Photon-photon interaction

Photons in linear media do not interact



Effective photon-photon interaction exploiting the *nonlinearity of the atoms*



We measure a linear response!

# III Rydberg atoms: why?

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Even if an atom is a highly nonlinear object, the nonlinearity is very hard to be measured: it is LOCAL in space and NARROW in time.



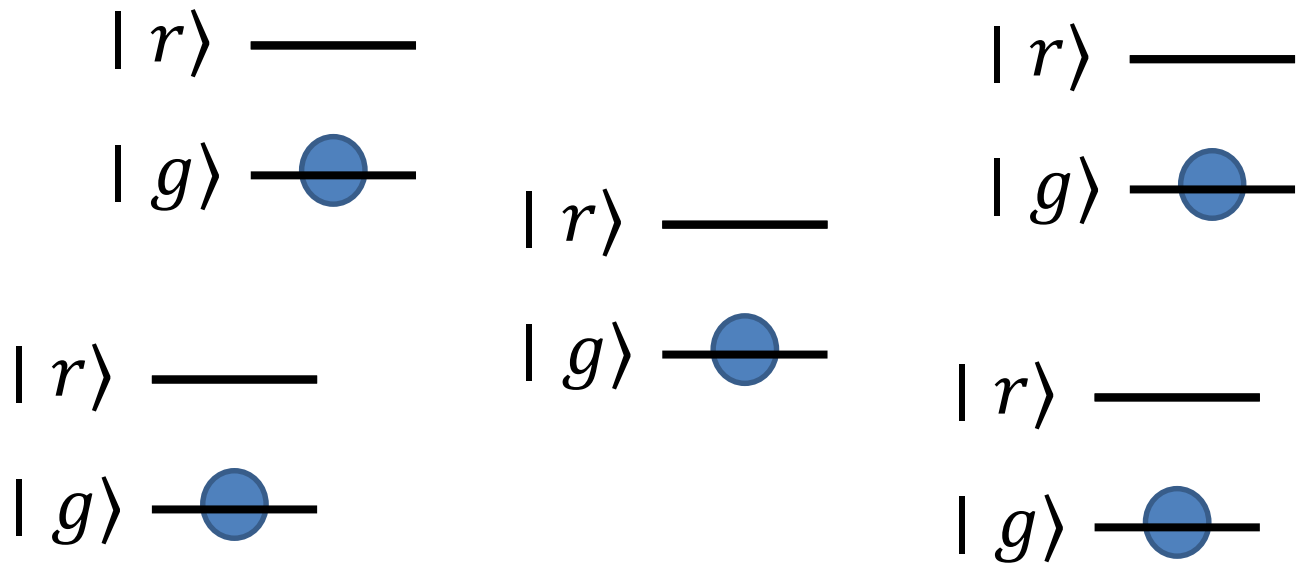
A **Rydberg atom** is an atom excited to a *high principal quantum number state*. These states exhibit a very long lifetime and a **huge dipole momentum**, able to shift the energy levels of the surrounding atoms, within the **blockade sphere**.



A **Rydberg atom** acts as a ‘**super atom**’. It provides a NONLOCAL blockade mechanism able to introduce an effective nonlinear photon-photon interaction.

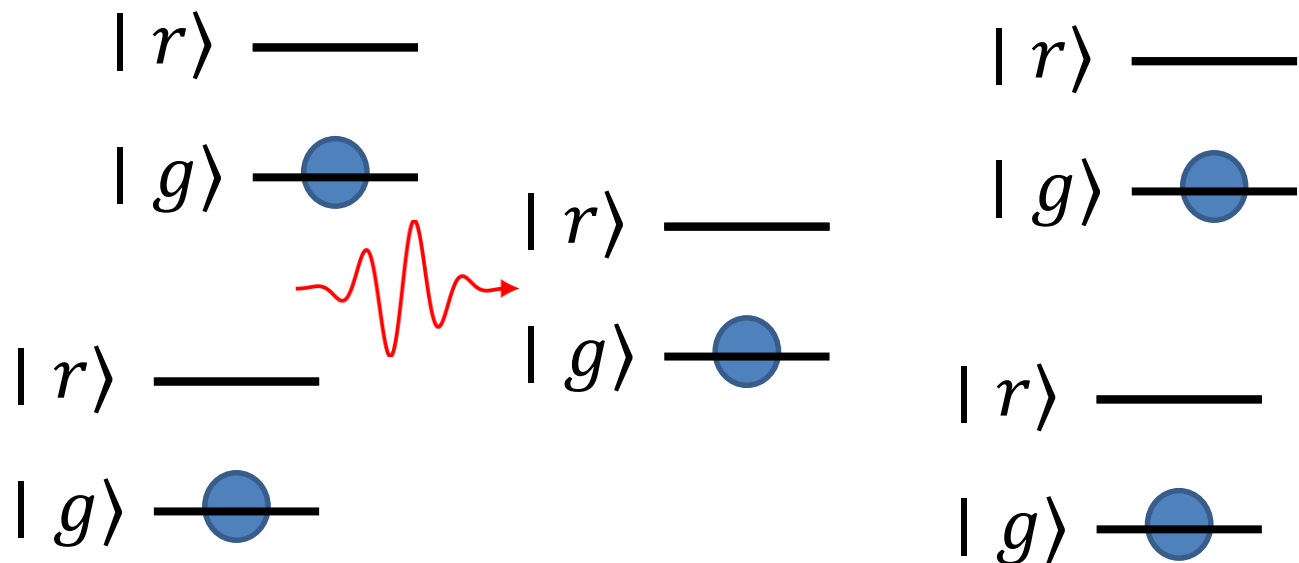
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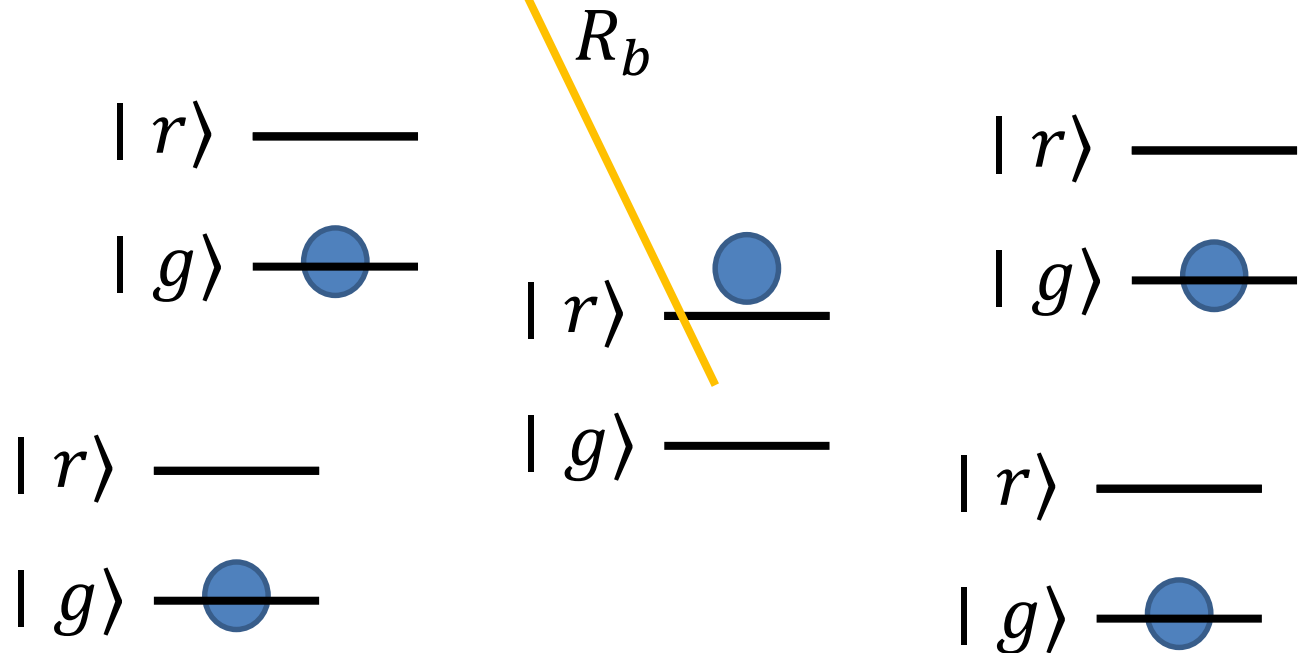
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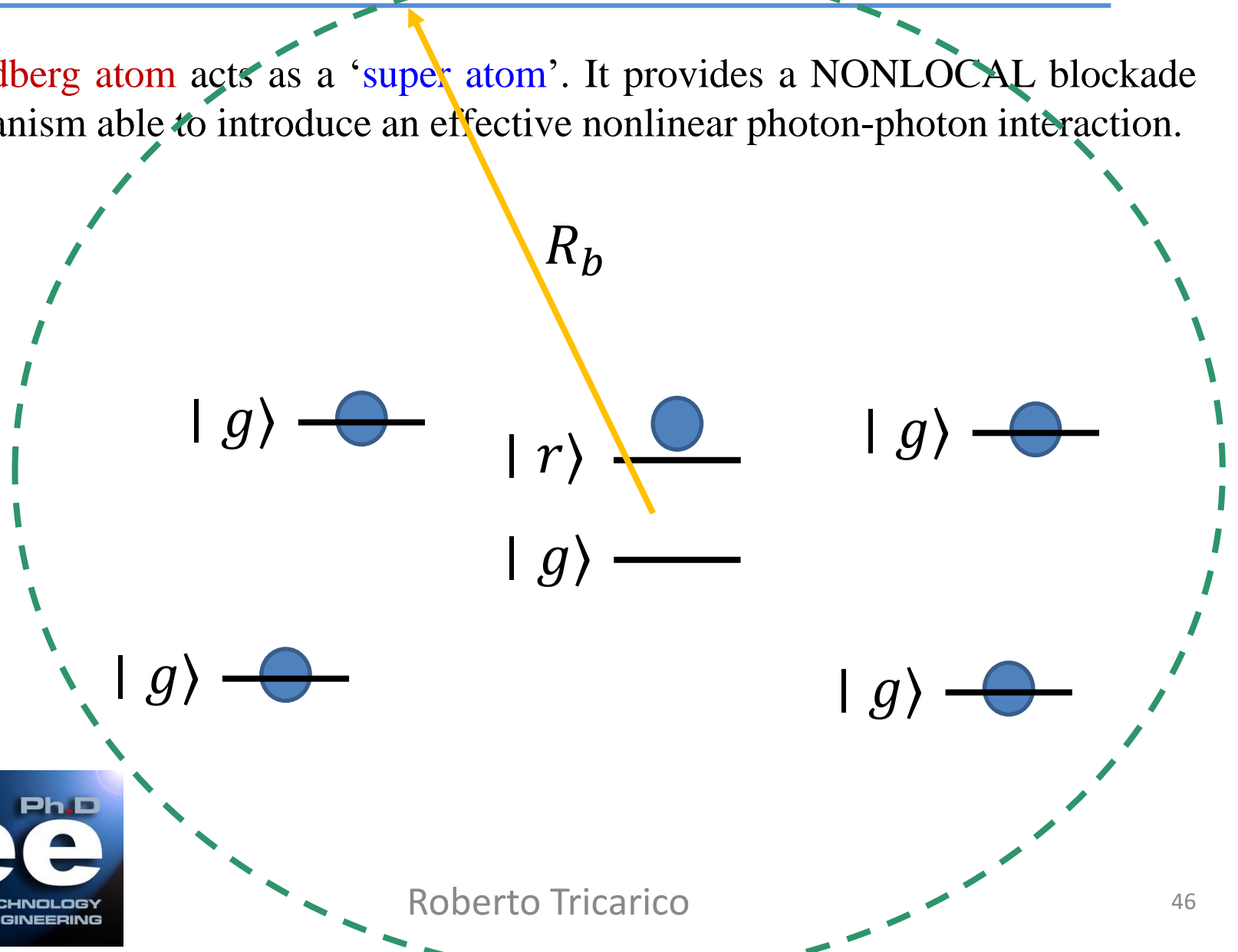
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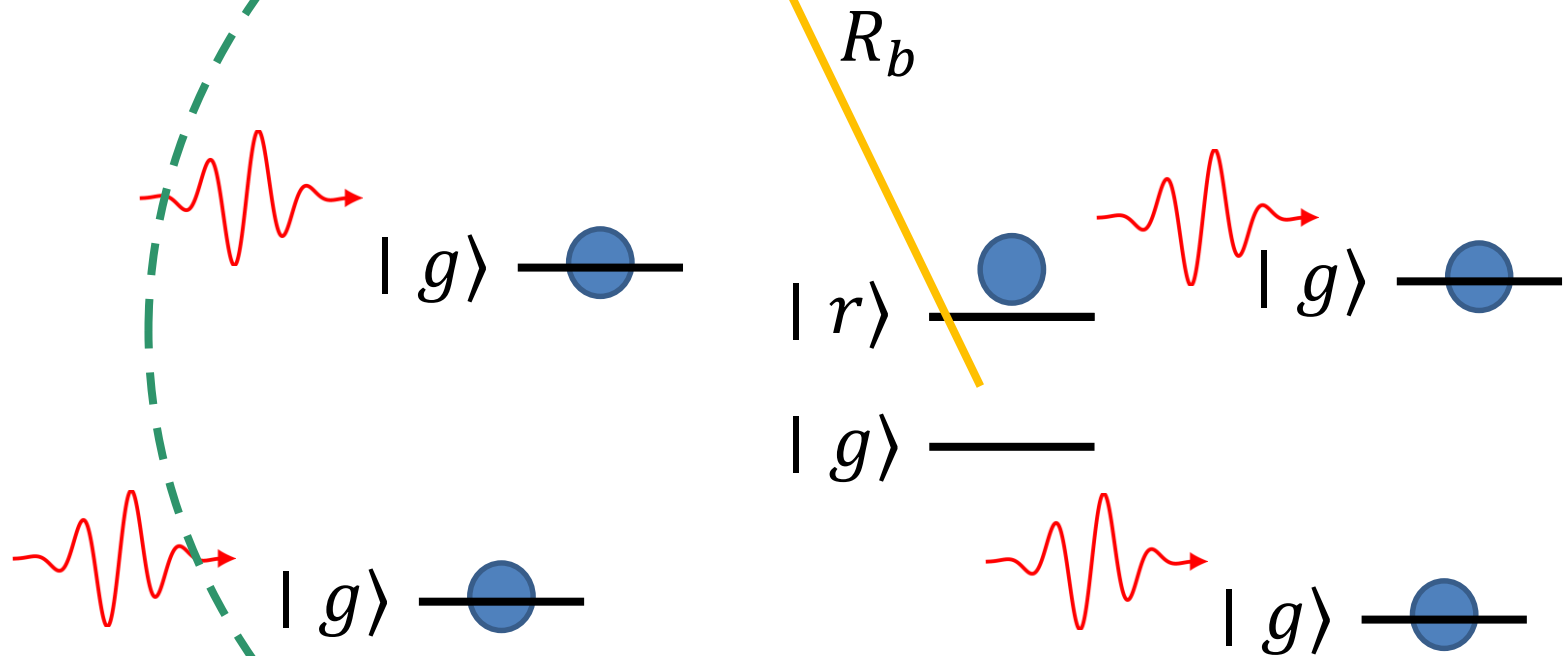
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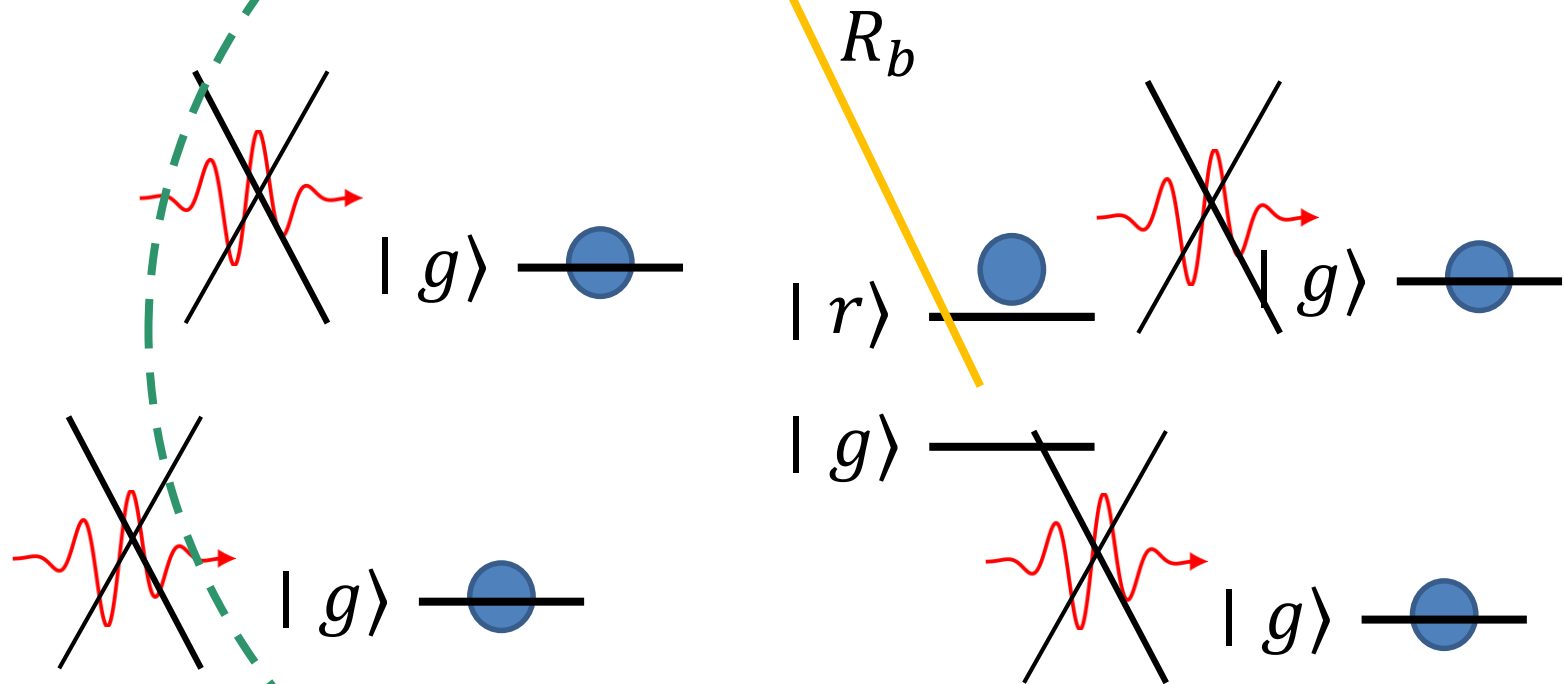
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# III Rydberg atoms: why?

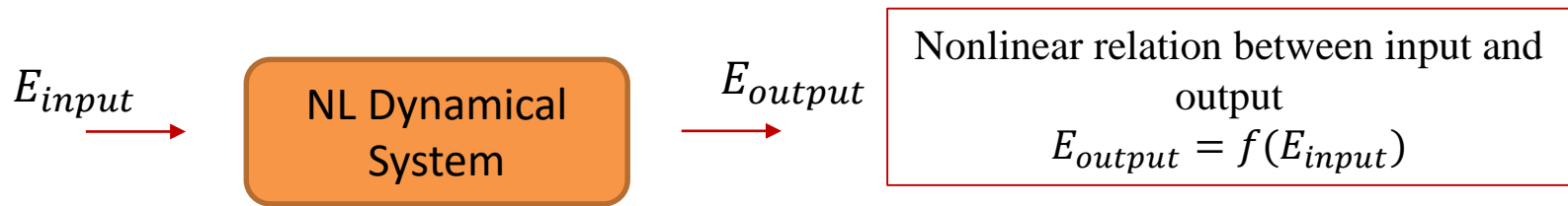
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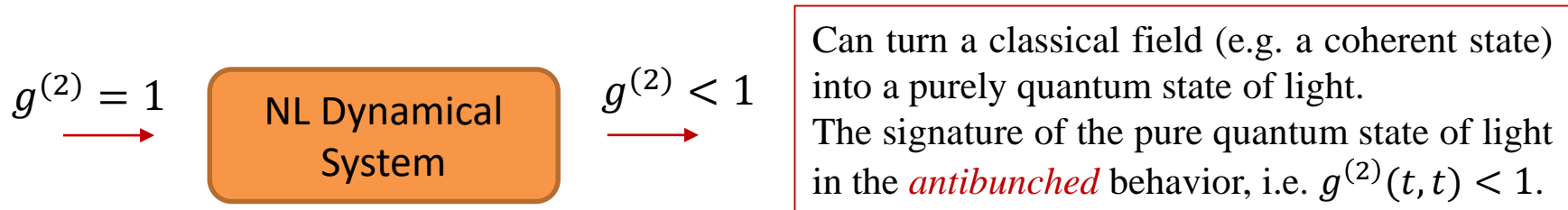


# III How to quantify nonlinearity?

- Classical Point of view



- Quantum point of view

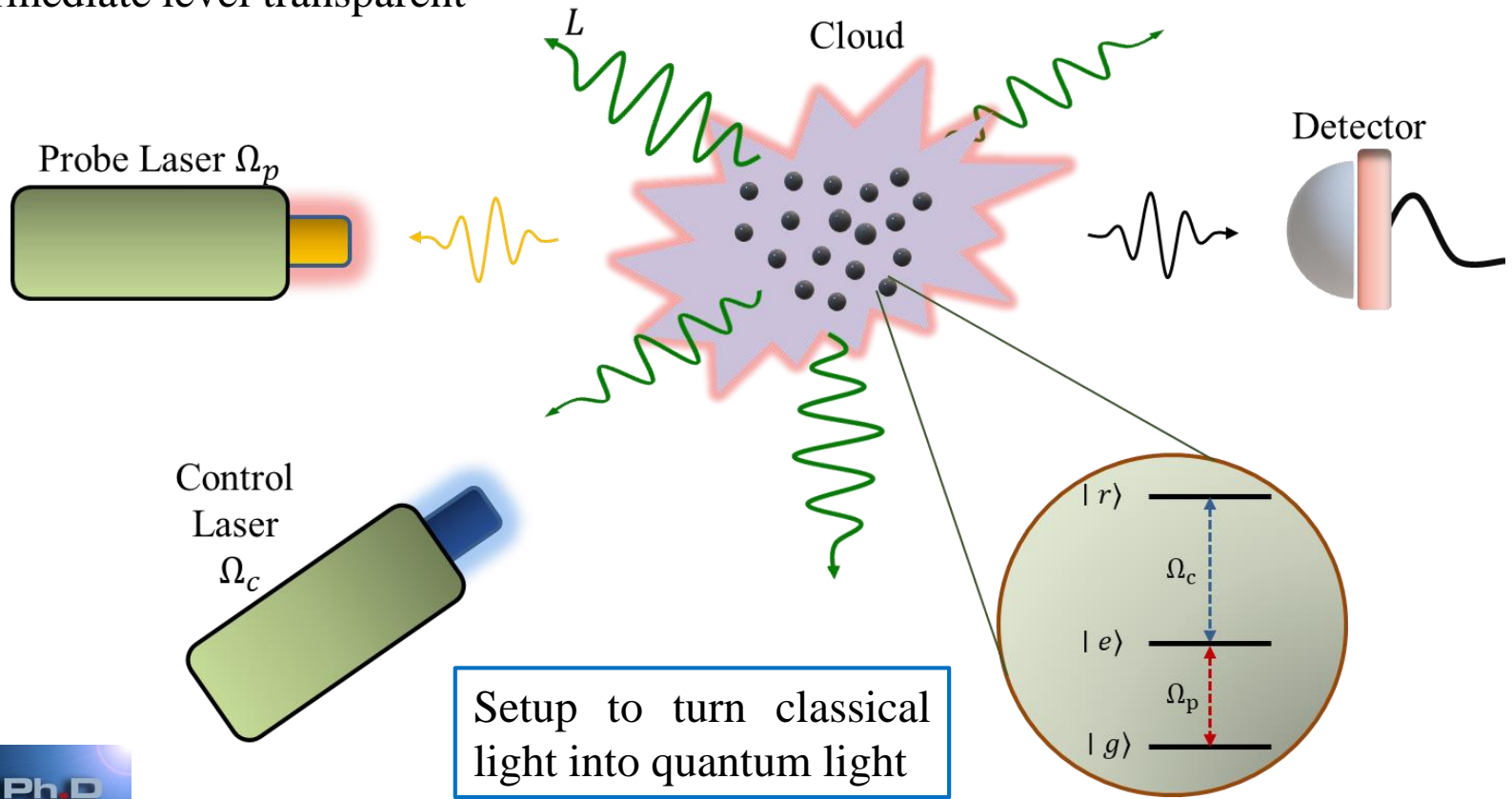


$$g^{(2)}(t, t') = \frac{\langle \psi | E^-(t) E^-(t') E^+(t') E^+(t) | \psi \rangle}{\Omega^4 \langle \psi | E^-(t) E^+(t) | \psi \rangle \langle \psi | E^-(t') E^+(t') | \psi \rangle}, \quad (t' \geq t)$$

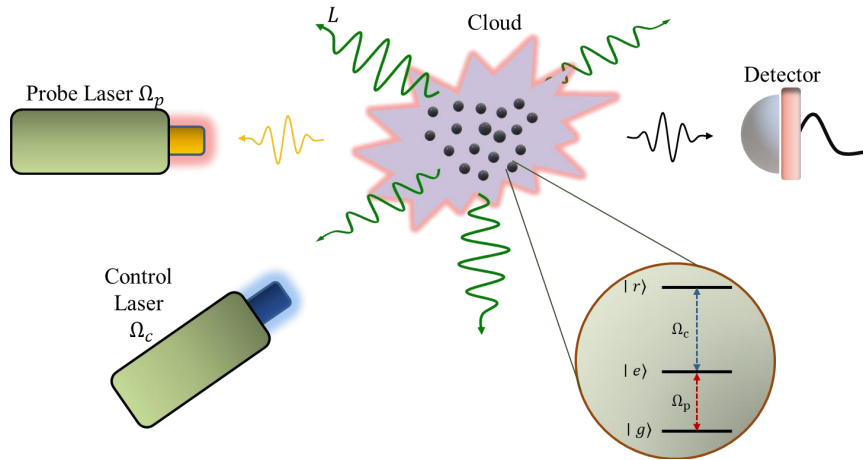
# III Rydberg-EIT

EIT= Electromagnetic Induced Transparency

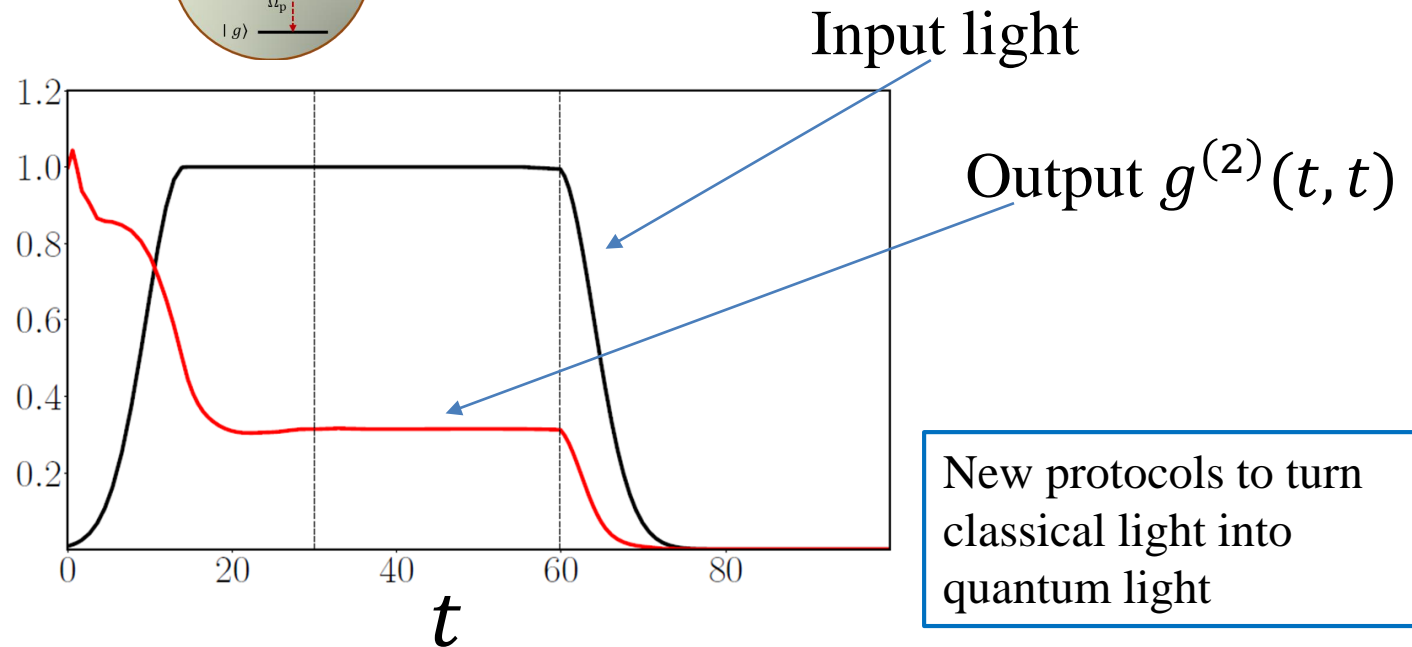
It is a 3-level scheme, where an inference phenomenon between 2 shining laser makes the intermediate level transparent

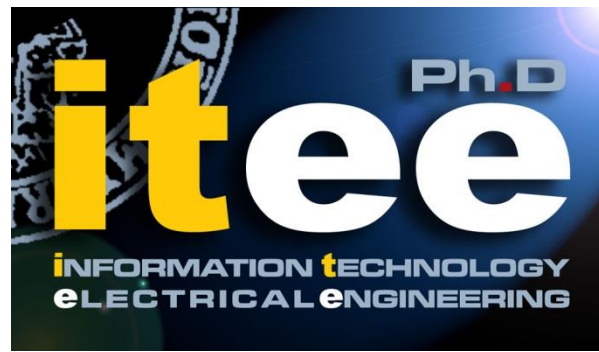


# III Nonlinearities in R-EIT



I theoretically modelled the experimental measurements of C. Adams' group (2019) which showed that the **pulse dynamics** can be more antibunched than the steady state one.





# THANK YOU

Roberto Tricarico

Light-Matter Interaction in Open  
Systems: from Nanoparticles to  
Atoms



UNIVERSITÀ DEGLI STUDI DI NAPOLI  
FEDERICO II